Package ‘fso’

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Title Fuzzy Set Ordination

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Description Fuzzy set ordination is a multivariate analysis used in ecology to relate the composition of samples to possible explanatory variables. While differing in theory and method, in practice, the use is similar to 'constrained ordination.' The package contains plotting and summary functions as well as the analyses

Depends labdsv, rgl

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**Fuzzy Set Ordination**

**Description**

Computes a fuzzy set for samples along a specified environmental or experimental gradient based on sample similarities and gradient values as weights. The fuzzy set memberships represent the degree to which a sample is similar to one end of the gradient while not similar to the other.

**Usage**

```r
## S3 method for class 'formula'
fso(formula, dis, data, permute = FALSE, ...)
## Default S3 method:
fso(x, dis, permute = FALSE, ...)
## S3 method for class 'fso'
summary(object, ...)
```

**Arguments**

- `formula` a formula in the form of ~x+y+z (no LHS)
- `dis` a dist object such as that returned by `dist`, `dsvdis`, or `vegdist`
- `data` a data frame that holds variables listed in the formula
- `permute` if FALSE, estimate probabilities from Z distribution for correlation; if numeric, estimate probabilities from permutation of input
- `x` a numerical vector, a matrix, or numeric dataframe
- `object` an object of class ‘fso’
- `...` generic arguments for future use

**Details**

The algorithm converts the input to a full symmetric similarity matrix and bounds [0,1] (if necessary). It then calculates several fuzzy sets:

\[
\mu_a(i) = \frac{(x_i - \text{min}(x))}{(\text{max}(x) - \text{min}(x))}
\]

\[
\mu_b(i) = 1 - \mu_a(i)
\]

\[
\mu_c(i) = \left( \sum_{j \neq i} \mu_a(j) \times y_{ij} \right) / \sum_{j \neq i} \mu_a(j)
\]

\[
\mu_d(i) = \left( \sum_{j \neq i} \mu_b(j) \times y_{ij} \right) / \sum_{j \neq i} \mu_b(j)
\]

\[
\mu_e(i) = \left( 1 + \left( \mu_d(i) \right)^2 - \left( \mu_c(i) \right)^2 \right) / 2
\]

where \(y_{i,j}\) is the similarity of sample \(i\) to sample \(j\).
A separate fuzzy set ordination is calculated for each term in the formula. If x is a matrix or dataframe a separate fuzzy set ordination is calculated for each column or field.

If permute is numeric, the permutation is performed permute-1 times, and the probability is estimated as \((\text{correlations} \geq \text{observed} + 1)/\text{permute}\)

**Value**

An object of class ‘fso’ which has the following elements:

- **mu**
  - the fuzzy membership values for individual plots in the fuzzy set. If x is a matrix or dataframe then mu is also a matrix of the same dimension.

- **data**
  - a copy of data vector or matrix y

- **r**
  - the correlation between the original vector and the fuzzy set. If x is a matrix or dataframe then r is a vector with length equal to the number of columns in the matrix or dataframe.

- **p**
  - the probability of obtaining a correlation between the data and fuzzy set as large as observed

- **d**
  - the correlation of pair-wise distances among each fuzzy set compared to the dissimilarity matrix from which the fso was constructed

- **var**
  - the variable name(s) from matrix y

**Note**

Fuzzy set ordination is a method of multivariate analysis employed in vegetation analysis.

fso can be run with the first argument either a dataframe or a formula (with no left hand side). The formula version has distinct advantages:

1) The data= argument allows the user to specify a data frame containing the variables of interest. In this way variables need not be local.

2) The formula version handles categorical variables by converting them to dummy variables. In the default version, all variables must be quantitative or binary.

3) The formula version is somewhat more graceful about handling missing values in the data.

**Author(s)**

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**References**


**Examples**

```r
library(labdsv)
data(bryceveg)
data(brycesite)
dis <- dsvdis(bryceveg,'bray/curtis')
elev.fso <- fso(brycesite$elev,dis)
elev.fso <- fso(~elev,dis,data=brycesite)
plot(elev.fso)
summary(elev.fso)
```

---

**mfso**

*Multidimensional Fuzzy Set Ordination*

**Description**

A multidimensional extension of fuzzy set ordination (FSO) that constructs a multidimensional ordination by mapping samples from fuzzy topological space to Euclidean space for statistical analysis. MFSO can be used in exploratory or testing modes.

**Usage**

```r
## S3 method for class 'formula'
mfso(formula,dis,data,permute=FALSE,lm=TRUE,scaling=1,...)
## Default S3 method:
mfso(x,dis,permute=FALSE,scaling=1,lm=TRUE,notmis=NULL,...)
## S3 method for class 'mfso'
summary(object,...)
```

**Arguments**

- **formula**: Model formula, with no left hand side. Right hand side gives the independent variables to use in fitting the model.
- **dis**: a `dist` object of class ‘dist’ returned from `dist`, `vegdist`, or `dsvdis`.
- **data**: a data frame containing the variables specified in the formula.
- **permute**: a switch to control how the probability of correlations is calculated. `permute=FALSE` (the default) uses a parametric Z distribution approximation; `permute=n` permutes the independent variables `(permute-1)` times and estimates the probability as `(m+1)/(permute)` where `m` is the number of permuted correlations greater than or equal to the observed correlation.
- **lm**: a switch to control scaling of axes after the first axis. If `lm=TRUE` (the default) each axis is constructed independently, and then subjected to a Gram-Schmidt orthogonalization to all previous axes to preserve only the the variability that is uncorrelated with all previous axes. If `lm=FALSE`, the full extent of all axes is preserved without correcting for correlation with previous axes.
mfso

scaling a switch to control how the initial fuzzy set axes are scaled: 1 = use raw \( \mu \) membership values, 2 = relativize \( \mu \) values \([0,1]\), 3 = relativize \( \mu \) values \([0,1]\) and multiply by respective correlation coefficient.

x a quantitative matrix or dataframe. One axis will be fit for each column

notmis a vector passed from the formula version of mfso to control for missing values in the data

object an object of class ‘mfso’

... generic arguments for future use

Details

mfso performs individual fso calculations on each column of a data frame or matrix, and then combines those fso axes into a higher dimensional object. The algorithm of fuzzy set ordination is described in the help file for fso. The key element in mfso is the Gram-Schmidt orthogonalization, which ensures that each axis is independent of all previous axes. In practice, each axis is regressed against all previous axes, and the residuals are retained as the result.

Value

an object of class ‘mfso’ with components:

mu a matrix of fuzzy set memberships of samples, analogous to the coordinates of the samples along the axes, one column for each axis
data a dataframe containing the independent variables as columns
r a vector of correlation coefficients, one for each axis in order
p a vector of probabilities of observing correlations as high as observed
var a vector of variables names used in fitting the model
gamma a vector of the fraction of variability for an axis that is independent of all previous axes

Note

MFSO is an extension of single dimensional fuzzy set ordination designed to achieve low dimensional representations of a dissimilarity or distance matrix as a function of environmental or experimental variables. Although it is not technically a ‘constrained ordination,’ in practice its use is similar to cca or rda.

If you set lm=FALSE, an mfso is equivalent to an fso, but the plotting routines differ. For an mfso, the plotting routine plots each axis against all others in turn; for an fso the plotting routine plots each axis against the environmental or experimental variable it is derived from.

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plot.fso

Plotting Routines for Fuzzy Set Ordinations

Description
A set of routines for plotting, highlighting points, or identifying the distribution of a third variable on an fso.

Usage

```r
# S3 method for class 'fso'
plot(x, which="all", xlab = x$var, ylab="mu(x)", title="", r=TRUE, pch=1, ...)
# S3 method for class 'fso'
points(x, overlay, which="all", col=2, cex=1, pch=1, ...)
# S3 method for class 'fso'
plotid(ord, which="all", xlab=ord$var, ylab="mu(x)", title="", r=TRUE, pch=1, labels=NULL, ...)
# S3 method for class 'fso'
hilight(ord, overlay, which=1, cols = c(2, 3, 4, 5, 6, 7), symbol = c(1, 3, 5), ...)
# S3 method for class 'fso'
chullord(ord, overlay, which = 1, cols = c(2, 3, 4, 5, 6, 7), ltys = c(1, 2, 3), ...)
# S3 method for class 'fso'
boxplot(x, ...)
```

References
http://ecology.montana.msu.edu/R/labds/1abs/lab11/lab11.html

See Also
cca, capscale

Examples

```r
require(labdsv)
data(bryceveg) # returns a vegetation dataframe
data(brycesite) # returns a dataframe of environmental variables
dis.bc <- dsvis(bryceveg, 'bray/curtis')
# returns an object of class sQuote{dist}
demo.mfso <- mfso(~elev+slope+av, dis.bc, data=brycesite) # creates the mfso
summary(demo.mfso)
## Not run: plot(demo.mfso)
```
**plot.fso**

**Arguments**

- **x**: an object of class ‘fso’
- **ord**: an object of class ‘fso’
- **which**: a switch to control which axis is plotted
- **r**: a switch to control printing the correlation coefficient in the plot
- **fso**: an object of class ‘fso’ from `fso`
- **overlay**: a logical vector of the same length as the number of points in the plot
- **labels**: a vector of labels to print next to the identified points
- **symbol**: an integer or vector of integers to control which symbols are printed in which order on the plot by specifying values to `pch`
- **ltys**: an integer or vector of integers to control the line styles of convex hull polygons
- **xlab**: text label for X axis
- **ylab**: text label for Y axis
- **title**: an overall title for the plot (equivalent to main)
- **pch**: the symbol for plotting
- **col**: the color for plotted symbols
- **cex**: the character expansion factor (font size)
- **cols**: an integer vector specifying color order
- **...**: arguments to pass to the underlying plot function

**Details**

Fuzzy set ordinations (FSO) are almost inherently graphical, and routines to facilitate plotting and overlaying are essential to work effectively with them.

A fuzzy set ordination object (an object of class ‘fso’) may contain one or more axes. In the simplest case, for a single-axis fso, the plot routine plots the underlying raw data on the X axis and the fuzzy set memberships on the Y axis, including by default the correlation coefficient in the upper left corner. For fsos containing multiple axes, the default (which="all") is to plot the raw data on the X axis, the respective fuzzy set memberships on the Y axis, plotting all axes in turn with a prompt to move to the next panel. This is often effective. It is also possible to plot a single panel out of the set of axes, specifying the axis as an integer with, e.g., “which = 2.”

The ‘points’ function can be used to highlight or identify specific points in the plot. The ‘points’ function requires a logical vector (TRUE/FALSE) of the same length as the number of points in the plot. The default behavior is to color the points with a respective TRUE value red. It is possible to control the color (with col=), size (with cex=) and symbol (with pch=) of the points.

The ‘plotid’ function can be used to label or identify specific points with the mouse. Clicking the left mouse button adjacent to a point causes the point to be labeled, offset in the direction of the click relative to the point. Clicking the right mouse button exits the routine. The default (labels=NULL) is to label points with the row number in the data.frame (or position in the vector) for the point. Alternatively, specifying a vector of labels (labels=) prints the respective labels. If the data were derived from a data.frame, the row.names of the data.frame are often a good choice, but the labels can also be used with a factor vector to identify the distribution of values of a factor in the ordination (but see hilight as well).
The `hilight` function identifies the factor values of points in the ordination, using color and symbols to identify unique values (up to 18 values by default). The colors and symbols used can be specified by the `cols=` and `symbol=` arguments, which should both be integers or integer vectors. The default of colors 2, 3, 4, 5, 6, 7 and symbols 1, 3, 5 shows well in most cases, but on colored backgrounds you may need to adjust `cols=`. If you have a factor with more than 18 classes you will need to augment the `symbol=` vector with more values.

The `chullord` function plots convex hulls around all points sharing the same value for a factor variable, and colors all points of that value to match. The convention on colors follows `hilight`.

The `boxplot` function plots boxplots of the $\mu$ membership values for the fuzzy sets in the `fso`.

Note

The plotting and highlighting routines for `fso` are designed to match the same routines for other ordinations in package `labdsv`.

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References


See Also

`plot.pco`, `points.pco`, `hilight.pco`, `chullord.pco`

Examples

```r
require(labdsv) # to obtain access to data sets and dissimilarity function
data(bryceveg) # vegetation data
data(brycesite) # environmental data
dis.bc <- dsvdis(bryceveg,'bray/curtis') # produce `{dQuote}dist` object
demo.fso <- fso(~elev+slope+av,dis.bc,data=brycesite)
## Not run: plot(demo.fso)
## Not run: hilight(demo.mfso,brycesite$quad)
```

Description

A set of routines for plotting, identifying, or highlighting points in a multidimensional fuzzy set ordination (MFSO).
Usage

## S3 method for class 'mfso'
plot(x, dis=NULL, pch=1, ax=NULL, ay=NULL, ...)
## S3 method for class 'mfso'
points(x, overlay, col=2, pch=1, ...)
## S3 method for class 'mfso'
plotid(ord, dis=NULL, labels=NULL, ...)
## S3 method for class 'mfso'
hilight(ord, overlay, cols = c(2, 3, 4, 5, 6, 7), symbol = c(1, 3, 5), ...)
## S3 method for class 'mfso'
chullord(ord, overlay, cols = c(2, 3, 4, 5, 6, 7), ltys = c(1, 2, 3), ...)
## S3 method for class 'mfso'
boxplot(x, ...)
## S3 method for class 'mfso'
thull(ord, var, grain, ax=1, ay=2, col=2, grid=50, nlevels=5, levels=NULL, lty=1, numitr=100, ...)
rg1.mfso(mfso, first=1, second=2, third=3, radius=0.0005, col=0, ...)

Arguments

x an object of class ‘mfso’
ax X axis number
ay Y axis number
ord an object of class ‘mfso’
mfso an object of class ‘mfso’
dis an object of class ‘dist’ from dist, dsvdis, or vegdist
overlay a logical vector of the same length as the number of points in the plot
labels a vector of labels to print next to the identified points
symbol an integer or vector of integers to control which symbols are printed in which
order on the plot by specifying values to pch
ltys an integer or vector of integers to control the line styles of convex hull polygons
pch the symbol to plot
col the color to use for plotted symbols
cols an integer vector for color order
var a variable to fit with a tensioned hull
grain the size of the moving window used to calculate the tensioned hull
grid the number of cells in the image version of the tensioned hull
nlevels the number of contour levels to plot the tensioned hull
levels a logical variable to control plotting the contours on the tensioned hull
lty the line type to use in drawing the contours
numitr
the number of random iterations to use to compute the probability of obtaining 
as small a tensioned hull as observed

first
the X axis in the 3-D rgl plot

second
the Y axis in the 3-D rgl plot

third
the Z axis in the 3-D rgl plot

radius
the radius of the spheres used to represent points in the rgl plot

... arguments to pass to function points

Details

Multidimensional fuzzy set ordinations (MFSO) are almost inherently graphical, and routines to 
facilitate plotting and overlaying are essential to work effectively with them.

A multidimensional fuzzy set ordination object (an object of class ‘mfso’) generally contains at 
least two axes, and may contain many more. By default, the plot routine plots all possible axis 
pairs in order. If ‘ax’ and ‘ay’ are specified only a single plot is produced with X axis ax and Y axis 
ay. If ‘dist’ object is passed with the ‘dis=’ argument, the final panel is a plot of the dissimilarity or 
distance matrix values on the X axis and the pair-wise ordination distances on the Y axis with the 
correlation coefficient in the upper left hand corner.

The ‘points’ function can be used to highlight or identify specific points in the plot. The ‘points’ 
function requires a logical vector (TRUE/FALSE) of the same length as the number of points in the 
plot. The default behavior is to color the points with a respective TRUE value red. It is possible to 
control the color (with col=), size (with cex=) and symbol (with pch=) of the points.

The ‘plotid’ function can be used to label or identify specific points with the mouse. Clicking the 
left mouse button adjacent to a point causes the point to be labeled, offset in the direction of the click 
relative to the point. Clicking the right mouse button exits the routine. The default (labels=NULL) 
is to label points with the row number in the data.frame (or position in the vector) for the point. 
Alternatively, specifying a vector of labels (labels=) prints the respective labels. If the data were 
derived from a data.frame, the row.names of the data.frame are often a good choice, but the labels 
can also be used with a factor vector to identify the distribution of values of a factor in the ordination 
(but see hilight as well).

The ‘hilight’ function identifies the factor values of points in the ordination, using color and symbols 
to identify unique values (up to 18 values by default). The colors and symbols used can be specified 
by the ‘col=’ and ‘symbol=’ arguments, which should both be integers or integer vectors. The 
default of colors 2, 3, 4, 5, 6, 7 and symbols 1, 3, 5 shows well in most cases, but on colored 
backgrounds you may need to adjust ‘col='. If you have a factor with more than 18 classes you will 
need to augment the ‘symbol=’ vector with more values.

The ‘chullord’ function plots convex hulls around all points sharing the same value for a factor 
variable, and colors all points of that value to match. The convention on colors follows hilight.

The ‘boxplot’ function plots boxplots of the $\mu$ membership values in the MFSO.

The ‘thull’ function drapes a tensioned hull for variable ‘var’ over the plotted mfso.

Value

none
**Step-Wise Forward Variable Selection in a Multivariate Fuzzy Set Ordination**

A simple routine to screen variables for addition to a multivariate fuzzy set ordination (MFSO). The routine operates by adding variables one at a time to an existing MFSO (which can be NULL), and calculating the correlation coefficient between the underlying dissimilarity matrix (object of class 'dist') and the pair-wise distances in the MFSO ordination.

**Usage**

```r
step.mfso(dis,start,add,numitr=100,scaling=1)
```

**Arguments**

- `dis` a dissimilarity of distance object from `dist`, `dsvdis`, or `vegdist` or other 'dist' object
- `start` either NULL (to find the first variable to add) or a data.frame of binary or quantitative variables to use in the base model
- `add` a data.frame of binary or quantitative variables to screen for addition to the model
- `numitr` the number of random permutations of a vector to use in establishing the probability of observing as large an increase in correlation as observed
- `scaling` the scaling parameter to pass along to `mfso`
Details

`mfso` is intended as a tool for analysis of multiple competing hypotheses, and the analyst is expected to have a priori models to compare. Nonetheless, `mfso` can be used in a hypothesis generating variable screening mode by maximizing the correlation between the underlying dissimilarity matrix and the pair-wise distances in the `mfso` ordination.

The `step.mfso` function is an inelegant approach to step-wise forward variable selection in `mfso`. It considers each variable offered in turn, calculates the `mfso` resulting from adding that variable to the given `mfso`, permutes that variable `numitr` times, and determines a probability of observing as large an increase in correlation as observed. After testing all variables for inclusion, it simply prints a table of the calculations, and the analyst has to rerun the routine adding the selected variable to data.frame `start` and deleting it from `add`.

While it would be nice to automate the production of the step-wise `mfso`, to date I have only implemented this limited function. In addition, model parsimony is ensured by the permutation routine, rather than an AIC-based approach, and doesn’t directly penalize for degrees of freedom (number of variables).

Value

Produces a table of the analysis but does not produce any objects

Author(s)

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References


Examples

```r
## Not run: require(labdsv) # make data available
## Not run: data(bryceveg) # get vegetation data
## Not run: data(brycesite) # get environmental data
## Not run: dis.bc <- dsvdis(bryceveg,'bray.curtis') # produce dist object
## Not run: attach(brycesite) # make variables easily available
## Not run: step.mfso(dis.bc,start=NULL,add=data.frame(elev,slope,av))
## Not run: step.mfso(dis.bc,start=data.frame(elev),add=data.frame(slope,av))
```
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